

$$y = \vec{w}^T \vec{x} \longrightarrow y = w_3 x^3 + w_2 x^2 + w_1 x + w_0$$

Linear regression

Polynomial regression

here we have a 1D input  
 $y = w_1 x + w_0$   
 ↑ scalar    ↑ scalar    scalar

Feature mappings

Define a feature map  $\phi(x) = \begin{pmatrix} 1 \\ x \\ x^2 \\ x^3 \end{pmatrix}$

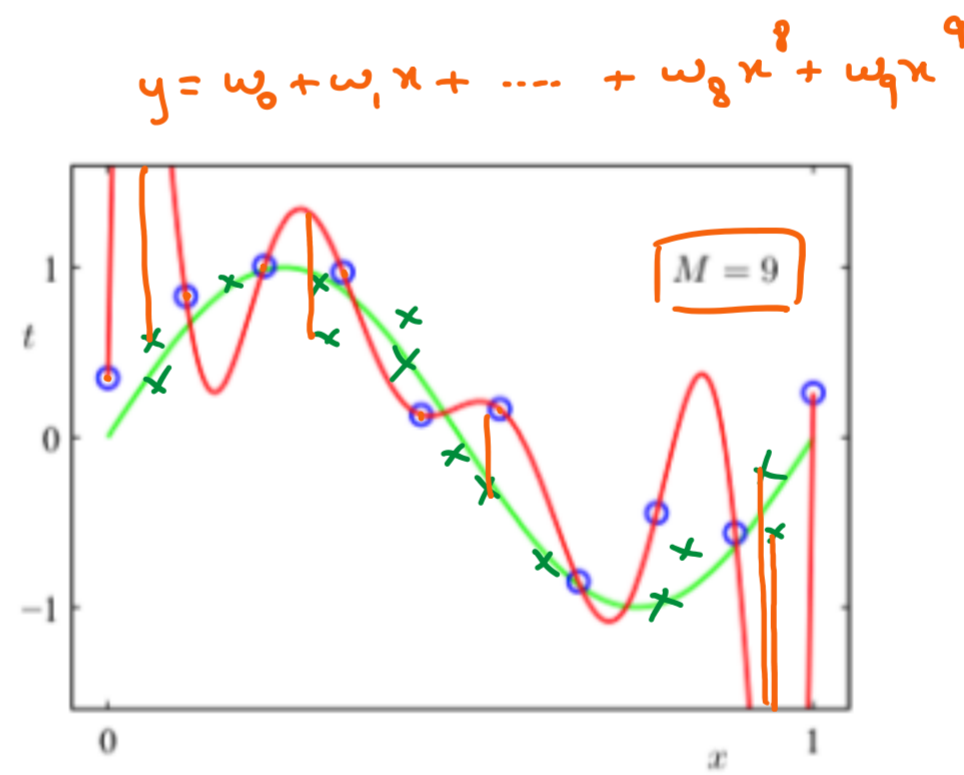
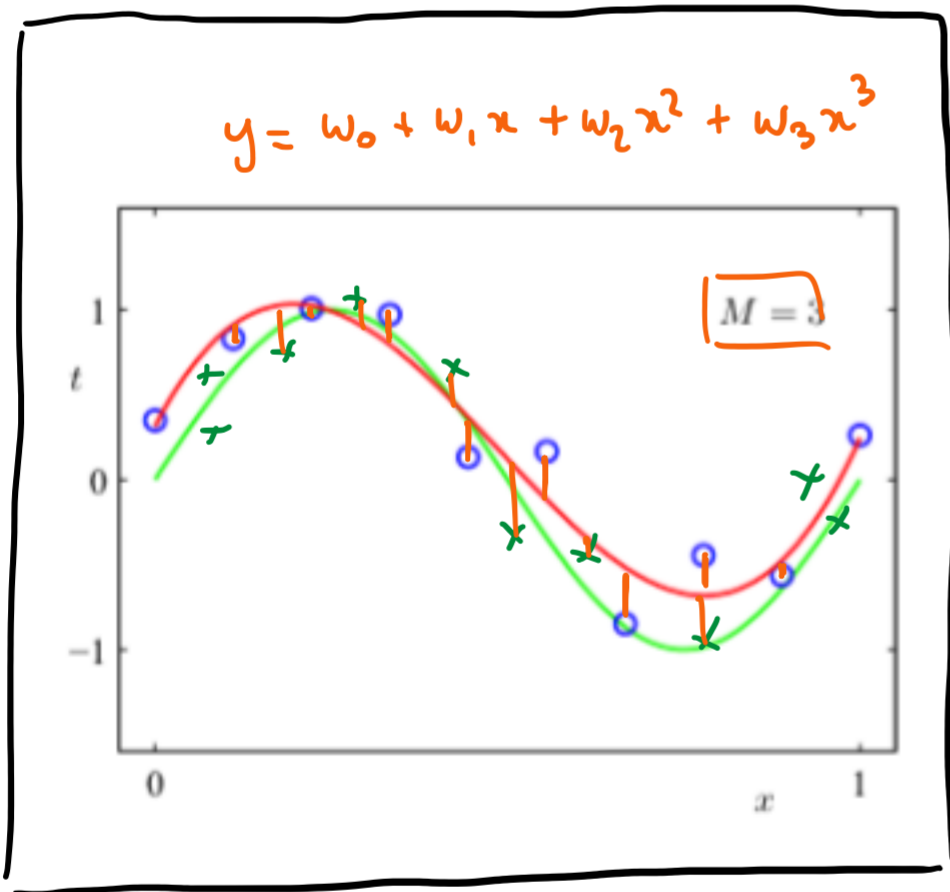
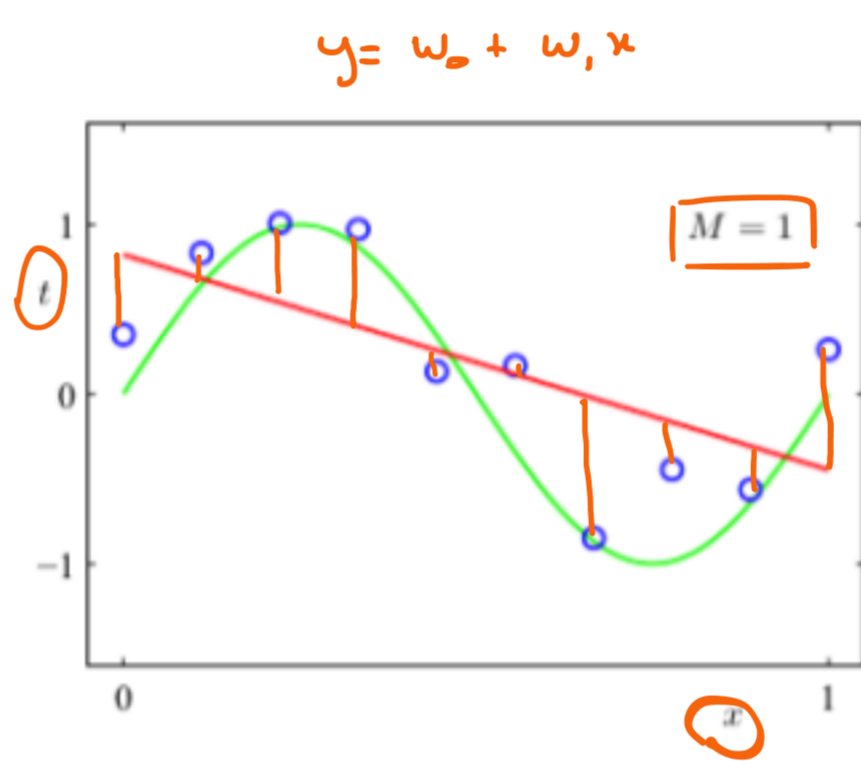
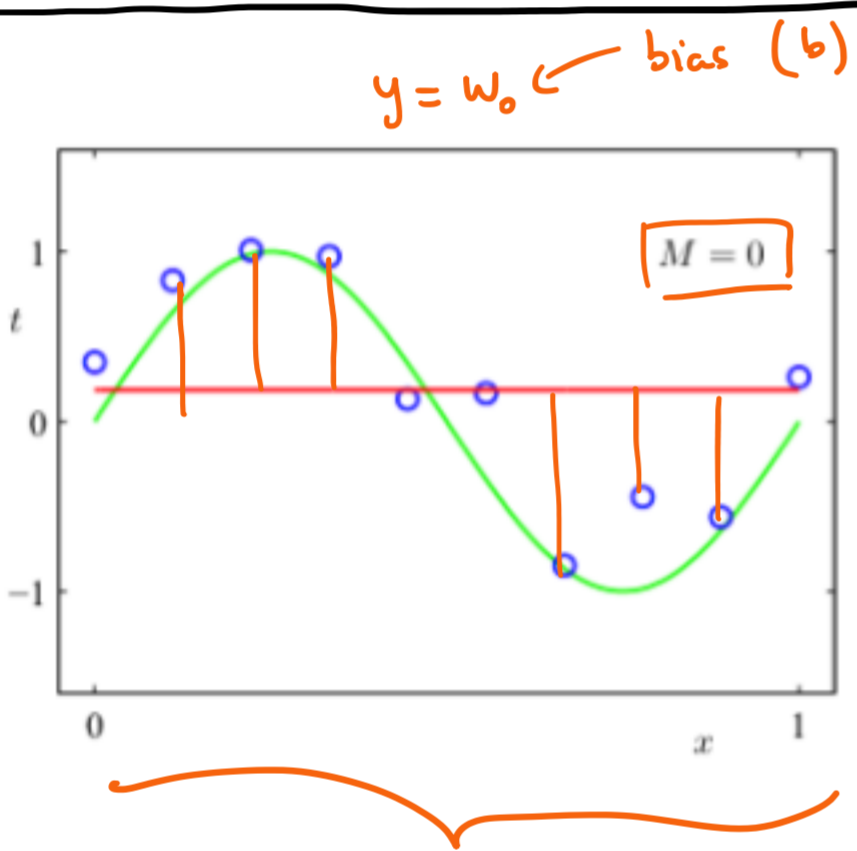
Define a polynomial regression model :

$$y = \vec{w}^T \phi(x)$$

vector because the feature map produces 4 components (features)

input  $x$  is replaced with the feature map.

How to choose the degree of the polynomial?



Adapted from Bishop (Pattern Recognition & ML)

Generalization

Hyperparameters : parameters which we can't include in the training itself  
 (e.g., the degree of the polynomial)

To tune hyperparameters, we will use a validation set.

